

## Abstract

Atmospheric neutrinos provide a powerful probe of physics due to the broad range of both energies and baselines. I will discuss exactly how they play the key role in constraining tau neutrino unitarity via a complex interplay of the matter effect, tau lepton production threshold, misreconstructed tau neutrino energy, and the matter effect. This allows one to identify tau neutrino with no event-by-event discrimination and without assuming unitarity. I will also discuss how low energy atmospheric neutrinos, which will be detected by DUNE, will probe the size of the Earth's core and the matter effect in the Earth.

# New Perspectives on Atmospheric Neutrinos

Peter B. Denton

INFN Torino

March 31, 2022

2109.14576

and

2110.01148 with Rebekah Pestes



# Overview

1. Unitarity constraints on tau neutrinos
2. Tau neutrino appearance in atmospheric neutrinos
3. Impact of different tau neutrino specific effects
4. Low energy atmospheric neutrinos at DUNE
5. Constraining the matter effect
6. Constraining the size of the Earth's core

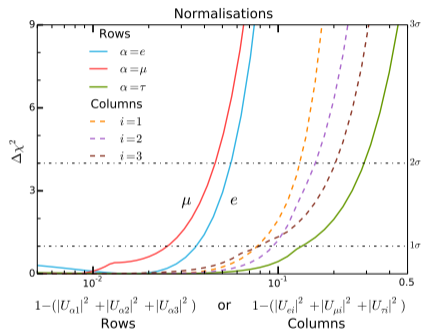
# Unitarity Constraints on Tau Neutrinos

Past studies used:

1.  $\nu_\mu \rightarrow \nu_\tau$  at OPERA
2. SNO NC and CC data

S. Ellis, K. Kelly, S. Li [2008.01088](#)

Z. Hu, J. Ling, J. Tang, T. Wang [2008.09730](#)



S. Parke M. Ross-Lonergan [1508.05095](#)

# More Tau Neutrinos!

The global tau neutrino data set:

Experiment	Source	$\sim$ Events detected
DONuT	Production	7.5
OPERA	Long-baseline	8
SK	Atmospheric	291
IceCube	Atmospheric	1804 <sup>1</sup>
IceCube	Astrophysical	2

<sup>1</sup>with  $\sim 10$ k en route soon, see J. Koskinen [IceCube NuTau2021 talk](#)

Dominant unitarity constraint comes from atmospheric  $\nu_\tau$  appearance

[PBD](#), J. Gehrlein [2109.14575](#)

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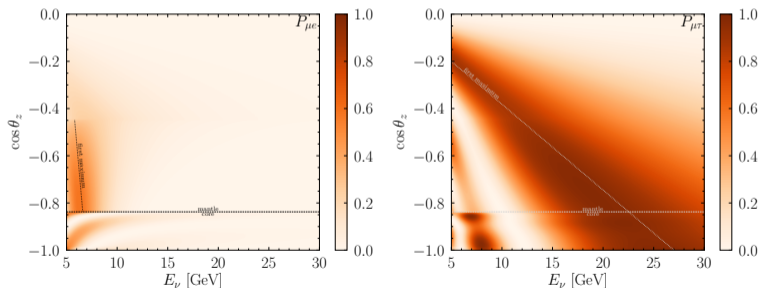
[PBD](#), J. Gehrlein [2109.14575](#)

A word on solar neutrinos:

1. SK 1998: showed that  $\nu_\mu$ - $\nu_\tau$  mixing is large
2. SNO 2001,2002: ES and NC measured a statistically significant non- $\nu_e$  flux
3.  $\Rightarrow \nu_e \rightarrow \nu_\tau$  at SNO with input from SK

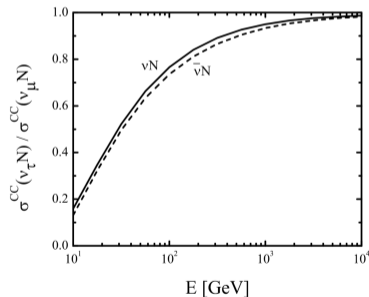
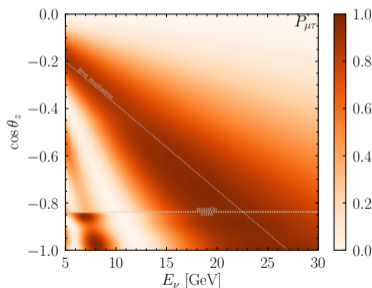
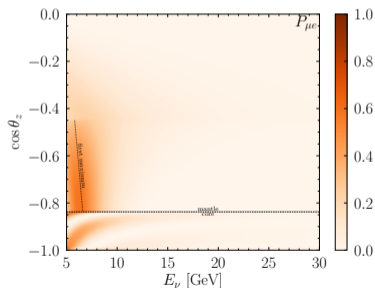
# Atmospheric Tau Neutrino Appearance

- ▶ Atmospheric neutrinos begin as  $\nu_\mu$  and mostly oscillate away to  $\nu_\tau$



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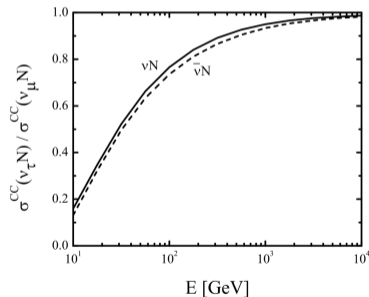
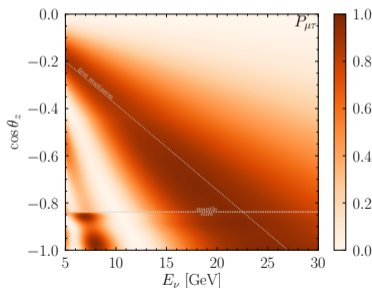
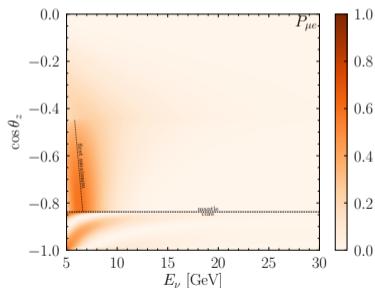


Y. Jeong, M. Reno [1007.1966](#)



# Atmospheric Tau Neutrino Appearance

- ▶ Atmospheric neutrinos begin as  $\nu_\mu$  and mostly oscillate away to  $\nu_\tau$
- ▶ High tau lepton production threshold diminishes events
- ▶ Identifying tau lepton in large coarse detectors is hard

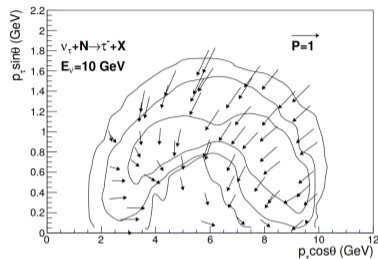


Y. Jeong, M. Reno [1007.1966](#)

# Tau Neutrino Appearance at SuperK

SuperK used:

1. Hadronic tau decay information
2. Tau polarization information
3. Neural net
4. *and standard oscillations*



# Tau Neutrino Appearance at SuperK

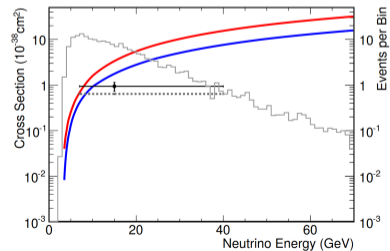
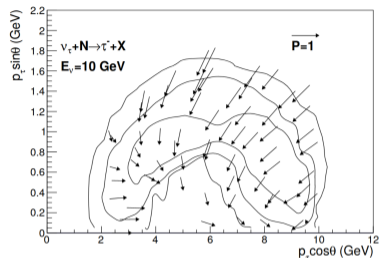
SuperK used:

1. Hadronic tau decay information
2. Tau polarization information
3. Neural net
4. *and standard oscillations*

Detected few hundred tau neutrino events,  
constrained the  $\nu_\tau$  “normalization”

e.g. weighted cross section:  $1.47 \pm 0.32 \times \text{SM}$

Super-KamiokaNDE [1711.09436](#)

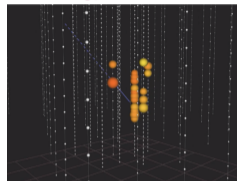


# Tau Neutrino Appearance at IceCube

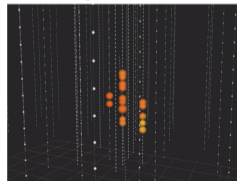
IceCube/DeepCore:

1. Much bigger than SuperK
2. 3D compared to SuperK's 2D
3. Much worse detector than SuperK
4. No ability to differentiate:
  - ▶  $\nu_\tau$  CC that goes to a muon
  - ▶  $\nu_\mu$  CCor
  - ▶  $\nu_\tau$  CC (that go to an electron or hadrons)
  - ▶  $\nu_e$  CC
  - ▶  $\nu$  NC

Track with  
energy of 26 GeV



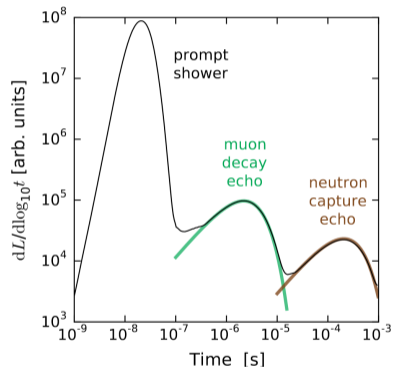
Cascade with  
energy of 30 GeV



M. Rodriguez [IceCube slides](#)

# Possible Means of Identifying Tau Neutrinos Event-By-Event

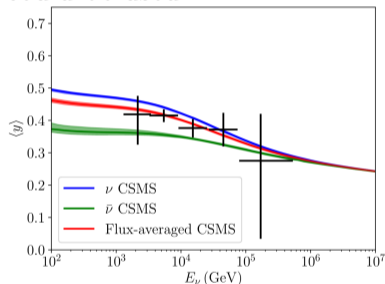
Hadronic showers contain far more muons and neutrons than electromagnetic showers



In practice, not possible

S. Li, M. Bustamante, J. Beacom [1606.06290](#)

Inelasticity correlates with  $E_\nu$  not  $E_{\text{dep}}$  and could be used

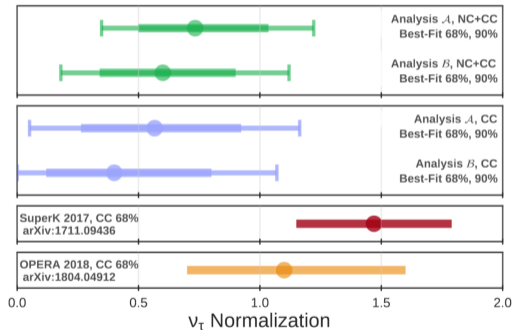
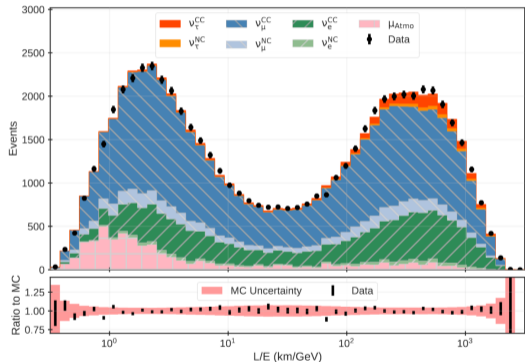


IceCube [1808.07629](#)

Too hard to measure at low energies

# IceCube Results

Using oscillation parameters IceCube finds:



IceCube [1901.05366](https://arxiv.org/abs/1901.05366)

## Past Work

Tau neutrino appearance in a large coarse detector is possible with:

1. Tau neutrino threshold
2. NC

T. Stanev [astro-ph/9907018](#)

Seeing extra low energy tau neutrinos could indicate astrophysical sources

H. Athar, F. Lee, G. Lin [hep-ph/0407183](#)

Both papers largely overlooked

# My Motivation

- ▶ Tau neutrino identification is relevant for unitarity

yet neither SuperK nor IceCube constrained unitarity with their data

- ▶ IceCube has the biggest data sets
- ▶ IceCube has extremely limited particle identification

cascades vs. tracks

- ▶ It would seem like  $\nu_\mu \rightarrow \nu_e$  could mimic  $\nu_\mu \rightarrow \nu_\tau$

For different oscillation parameters or with unitarity violation

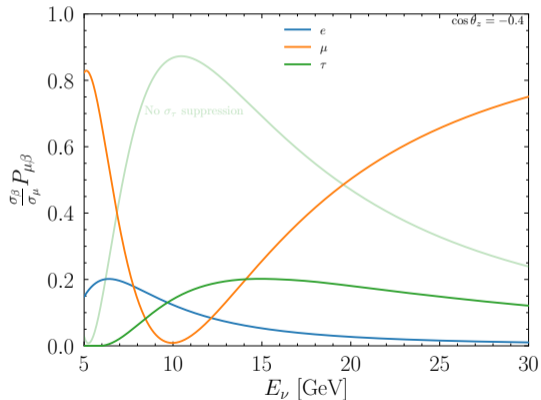
What, if any, physical effects allows for the identification of tau neutrinos without particle identification and without assuming unitarity?



# Mimicry Isn't Always Flattery

How to mimic  $\nu_\mu \rightarrow \nu_\tau$  with  $\nu_\mu \rightarrow \nu_e$  in the Earth:

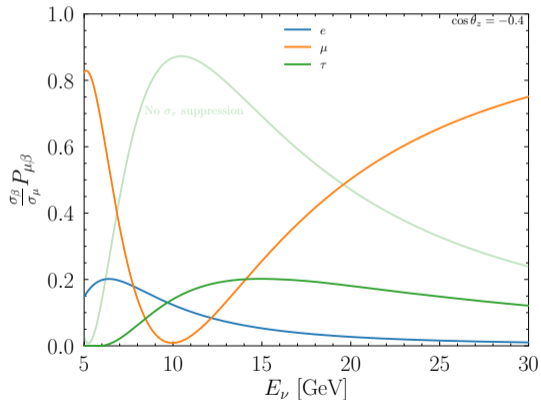
Through the mantle:



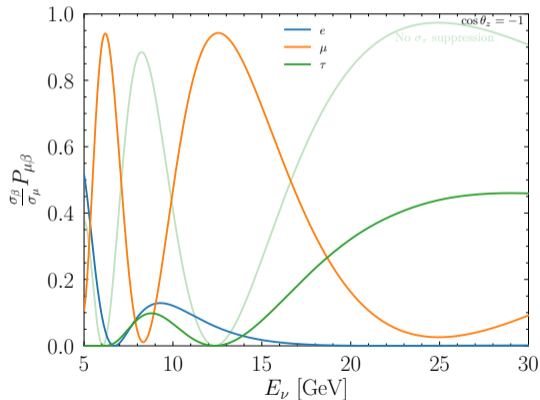
# Mimicry Isn't Always Flattery

How to mimic  $\nu_\mu \rightarrow \nu_\tau$  with  $\nu_\mu \rightarrow \nu_e$  in the Earth:

Through the mantle:



Through the core:



# Unitarity Violation Framework

- ▶ Suppose there are  $m$  total neutrinos and  $n$  kinematically accessible:  $(m, n)$ 
  - Accessible: [10 eV, 15 MeV]; inaccessible:  $\gtrsim 40$  MeV
  - $\nu_\tau$  is an exception to this that requires care
- ▶ Standard: (3,3)
- ▶ One accessible sterile: (4,4)
- ▶ Two heavy steriles: (5,3)
- ▶ Include matter effect
  - ▶ Steriles don't experience it - relevant for  $m = n$
  - ▶ It modifies the probability - relevant for  $m > n$
- ▶ For  $m = n$  oscillation probabilities can be calculated in the usual fashion
- ▶ For  $m > n$  care is required:
  - ▶ Flux, cross sections, and weak interaction need to be rescaled
  - ▶ Oscillation probability needs to be rescaled and carefully calculated:

$$P_{\alpha\beta}^r = \left| [N^* W e^{-i\Lambda L} W^\dagger N^T]_{\alpha\beta} \right|^2$$

$N$ :  $m \times m$  submatrix

$W, \Lambda$  eigenvectors/eigenvalues of Hamiltonian in mass basis with matter effect

# Back to IceCube Observables

Define this cascade ratio:

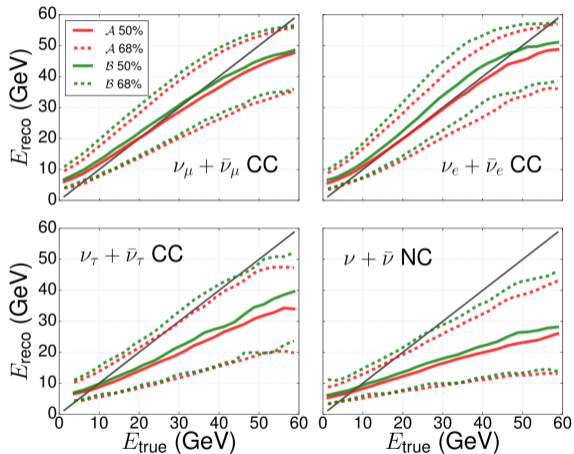
$$\mathcal{R}_c(E_{\text{reco}}, \cos \theta_z) \equiv \frac{\frac{d^2 N_c}{dE_{\text{reco}} d \cos \theta_z}}{\Phi_i(E_{\text{reco}}) \sigma_{\text{tot}}(E_{\text{reco}})}$$
$$= f_{\text{CC}} \left[ P_{\mu e}^r(E_{\text{reco}}, \cos \theta_z) + \eta_{\nu_\tau}^{\gamma-1} R_{\tau\mu}(E_{\text{reco}}/\eta_{\nu_\tau})(1 - f_{\tau\mu}) P_{\mu\tau}^r(E_{\text{reco}}/\eta_{\nu_\tau}, \cos \theta_z) \right]$$
$$+ (1 - f_{\text{CC}}) \eta_{\text{NC}}^{\gamma-1} \sum_{\beta \in \{e, \mu, \tau\}} P_{\mu\beta}^r(E_{\text{reco}}/\eta_{\text{NC}}, \cos \theta_z)$$

- ▶  $\nu_e$  CC appearance
- ▶  $\nu_\tau$  CC appearance with  $\tau \rightarrow \nu_\tau + (e, X)$
- ▶  $\tau$  production threshold
- ▶ Reconstructed energy shift from spectrum and cross section

Different for  $\tau \rightarrow \nu_\tau$  and NC

- ▶ NC

# Reconstructed vs. True Energy



$\tau$ 's always decay to invisible energy  $\nu_{\tau}$

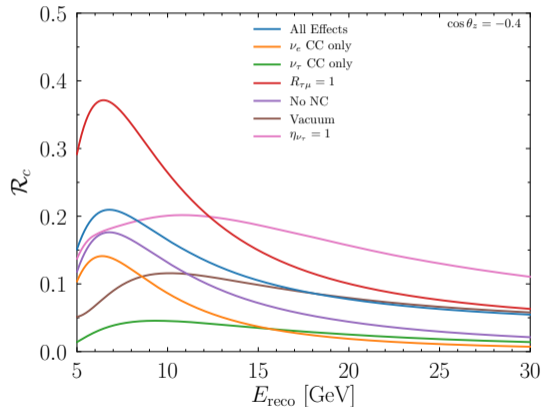
$$\eta_{\nu_{\tau}} = 0.625$$

NC always loses some energy

$$\eta_{\text{NC}} \simeq \frac{1}{3}$$

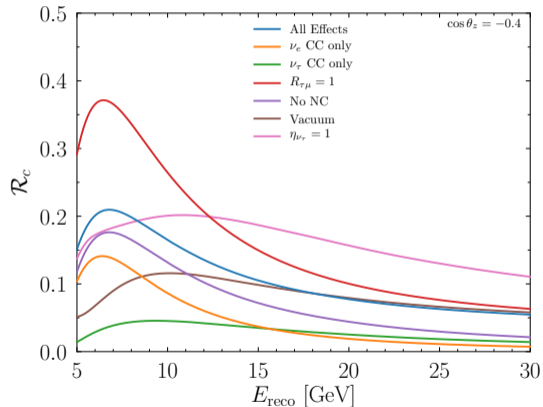
# Impact of Effects

Through the mantle:

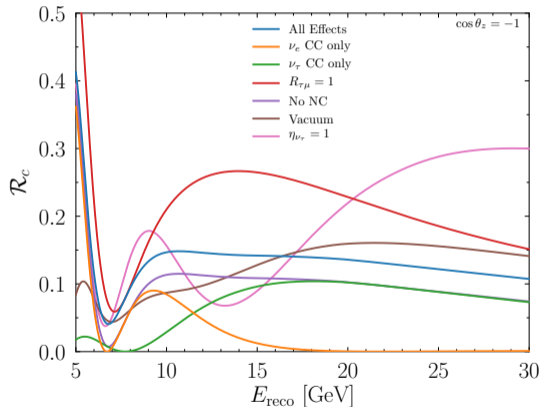


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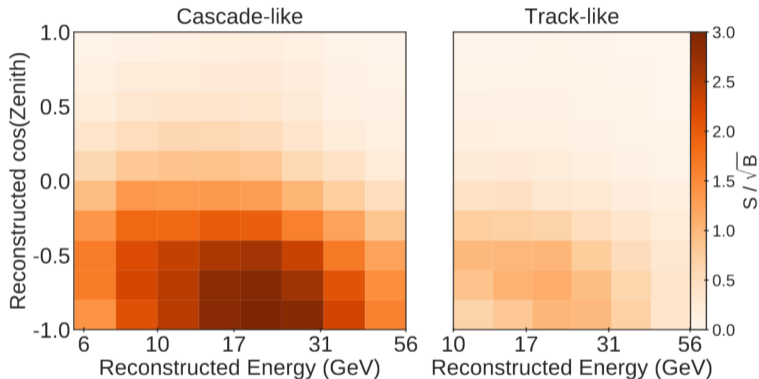
Through the mantle:



Through the core:



# IceCube Detector Sensitivities



Contains all information on detector efficiencies, flux, and track/cascade misidentification



# Results

Effects considered:

1. NC
2. Matter effect
3.  $\eta_{\nu_\tau}$ : Tau neutrino reconstruction
4.  $R_{\tau\mu}$ : Tau lepton production threshold
5. External  $\Delta m_{31}^2$  constraint
6. External  $\nu_e$  row constraint

Conclusions:

1. **With all known effects tau neutrinos can be identified even without assuming unitarity**
2. With all effects off and no unitarity:  $\nu_\tau$ 's cannot be identified.  
Dial up  $\nu_e$  to match
3. Including NC doesn't matter much
4. Turning on  $R_{\tau\mu}$ ,  $\eta_{\nu_\tau}$ , or the matter significantly enhances sensitivity
5. Certain combinations approximately cancel:  
Just  $R_{\tau\mu}$  and  $\eta_{\nu_\tau}$  has almost no sensitivity


# Atmospheric Appearance Unitarity Key Points

1. Conservatively didn't include down-going or tracks which add more information
2. Assume only oscillations,  $\tau$  properties, and the matter effect
3. Numerous effects allow for model independent detection of  $\nu_\tau$  with no event-by-event identification
4. Some of the effects actually partially cancel
5. Experiments can confidently report unitarity constraints

# Low Energy Atmospheric Neutrinos at DUNE

- ▶ DUNE should have sensitivity to low-E atmospheric neutrinos  $\nu_\mu \rightarrow \nu_e$   
DUNE [2002.03005](#)
- ▶ Lots of oscillation effects at  $E \in [100, 1000]$  MeV
- ▶ Modest sensitivity to  $\delta_{CP}$   
K. Kelly, et al [1904.02751](#)
- ▶ Modest sensitivity to mass ordering  
C. Ternes, et al [1905.03589](#)

Effects come from the Earth's core

A close-up shot of a man with dark hair and a mustache, looking off to the side with a serious, concerned expression. The scene is dimly lit with a strong green hue, suggesting a laboratory or a high-tech facility. The background is out of focus, showing some equipment and a bright light source.

It looks like the neutrinos coming from the sun  
have mutated into a new kind of nuclear particle.  
They're heating up the Earth's core

2012 the movie

# Earth's Core

Given that  $\delta_{CP}$  from T2HK and DUNE's accelerator program:  
Constrain the Earth's core?

Similar simultaneous paper: K. Kelly, et al [2110.00003](#)

- ▶ Most knowledge comes from seismographic data
- ▶ Inner core: solid, outer core: liquid  
from p- and s-waves
- ▶ Effects: Coriolis, Lorentz, self-excited dynamo, Alfvén waves, magnetic fields
- ▶ Outer core is surrounded by uncertain D'' layer  $\sim 200\text{km}$  thick

# Past Studies of the Earth with Neutrinos

## 1. Oscillation sensitivities:

- ▶ Focused on nuclear composition: fixing  $\rho$ , varying  $Z/A$  varies matter potential
- ▶ Considered PINGU and ORCA,  $E \in [1, 10]$  GeV

C. Rott, A. Taketa, D. Bose [1502.04930](#)

W. Winter [1511.05154](#)

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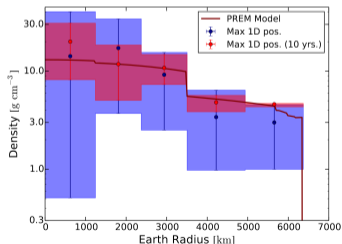
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C. Rott, A. Taketa, D. Bose [1502.04930](#)

W. Winter [1511.05154](#)

## 2. Absorption constraints:

- ▶ High energy neutrinos detected by IceCube are absorbed in the Earth
- ▶ Given the cross section and assuming isotropy



A. Donini, S. Palomares-Ruiz, J. Salvado [1803.05901](#)

# Matter Resonant Oscillation Physics

1. Matter effect: modifies oscillation parameters  $\Delta m_{ij}^2 \rightarrow \widehat{\Delta m}_{ij}^2$ ,  $\theta_{ij} \rightarrow \widehat{\theta}_{ij}$ ,  $\delta \rightarrow \widehat{\delta}$ 
  - ▶ Different for neutrinos and antineutrinos
  - ▶ Relevant for DUNE's mass ordering sensitivity

L. Wolfenstein [PRD 17, 2369 \(1978\)](#)

2. Adiabatic effect: start as  $\widehat{\nu}_i$  in matter, remain as  $\widehat{\nu}_i \rightarrow \nu_i$  in vacuum
  - ▶ Applies for a broad range of energies
  - ▶ The solution to the solar neutrino problem

S. Mikheyev, A. Smirnov, [SJNP 42, 913 \(1985\)](#)

S. Parke [PRL 57, 1275 \(1986\)](#)



# Matter Resonant Oscillation Physics

## 3. Resonant enhancement of a small mixing angle to maximal: $\widehat{\theta}_{ij} \rightarrow 45^\circ$

- ▶ Applies at one energy
- ▶ Relevant for sterile neutrino searches at IceCube

M. Chizhov, M. Maris, S. Petcov [hep-ph/9810501](#)

S. Mikheyev, A. Smirnov, SJNP 42, 913 (1985)

## 4. Parametric resonance: exponentially enhances a small mixing angle

- ▶ Works even for small absolute matter potential
- ▶ Requires specifically varying matter potential
- ▶ Only realistically relevant for the Earth's core

E. Akhmedov, SJNP 47, 301 (1988)

P. Krastev, A. Smirnov [PLB 226, 341 \(1989\)](#)

# Matter Resonances For Low Energy Atmospheric

For atmospheric neutrinos  $E \in [100, 1000]$  MeV:

1. Matter effect: mixing parameters are non-trivially modified
2. Adiabatic effect does not apply:  
neutrinos are produced in vacuum and experience discrete jumps in density
3. Resonant enhancement: occurs for solar parameters when

$$2\sqrt{2}G_F N_e E = \Delta m_{21}^2 \frac{\cos 2\theta_{12}}{c_{13}^2}$$

which is  $E \sim 130, 70, 35$  MeV in crust, mantle, and core

Crust is  $\cos \theta_z \in [-0.1, 1]$  but the first maximum is at  $-0.2$

Enhancement is  $33^\circ \rightarrow 45^\circ$  only a 20% increase

Only happens for relatively narrow energy range

# Parameter Matter Resonances For Low Energy Atmospheric

For some  $k_m, k_c$ , simultaneously satisfy

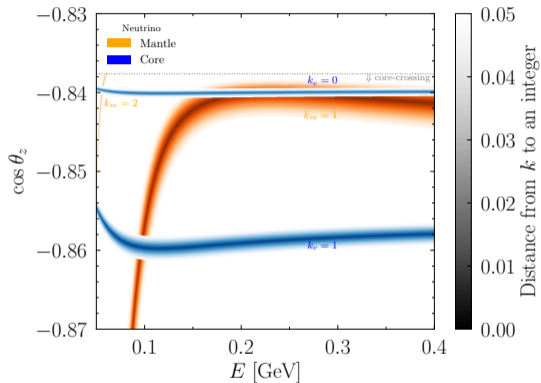
$$\left| \frac{\widehat{\Delta m_{21m}^2} L_m}{4E} \right| = \frac{\pi}{2} (2k_m + 1) \quad \text{and} \quad \left| \frac{\widehat{\Delta m_{21c}^2} L_c}{4E} \right| = \frac{\pi}{2} (2k_c + 1)$$

$\widehat{\Delta m_{21}^2}$  is  $\Delta m_{21}^2$  in matter

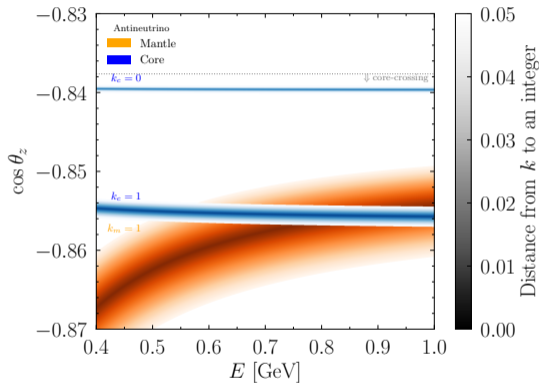
PBD, S. Parke [1902.07185](#)

# Parametric Resonances

## Neutrinos:



## Antineutrinos:

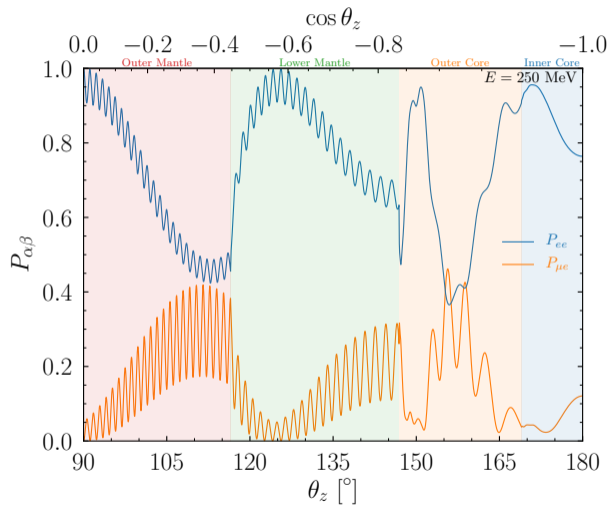


Largest region occurs for neutrinos  $E \sim 250$  MeV

Very narrow  $\cos \theta_z$  region

Blue curves separated by  $\sim 5 - 10^\circ$ : experimental resolution is  $\sim 10 - 20^\circ$

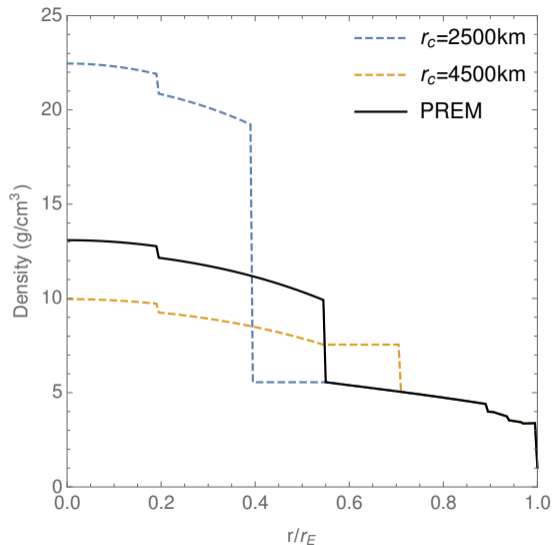
# Resonance Validation



# Varying the Earth's Core

- ▶ Fix the total mass
- ▶ Keep shape the same
- ▶ Shift the core radius
- ▶ Rescale the core density

Could also fix the inertia, we let it float



# Existing Constraints on the Matter Effect in the Earth

1. Solar matter effect: combine solar (SNO, Borexino, SK) and KamLand  
Slight tension, difficult solar measurements  $\Rightarrow \epsilon_{ee}^{\odot} \in [0, 1]$

SM:  $\epsilon = 0$

I. Esteban, et al [1805.04530](#)

P. Coloma, [PBD](#), et al [1701.04828](#)

2. In Earth: night time solar neutrinos at SK:  $1.9\sigma$  detection

Y. Nakajima [SK talk at Neutrino 2020](#)

3. Future: DUNE LBL:  $\sim 3\sigma$  sensitivity

K. Kelly, S. Parke [1802.06784](#)

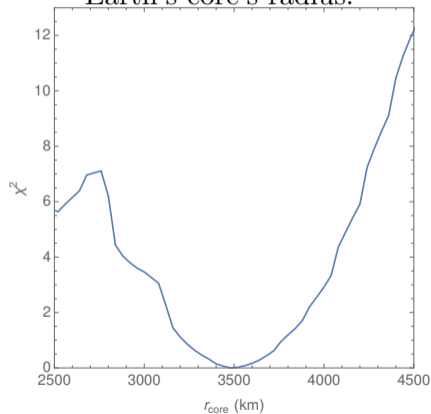
4. Future DUNE night time solar

F. Capozzi, et al [1808.08232](#)

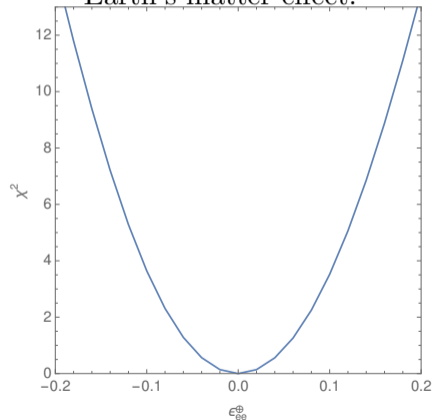
# Constraints

10 years of DUNE

Earth's core's radius:



Earth's matter effect:





# Final Core Thoughts

- ▶ Better understanding of the Earth's core connects with exoplanets
- ▶ Different measurements probe different things, relevant for DM accumulation:
  - L. Krauss, M. Srednicki, F. Wilczek, [PRD 33, 2079 \(1986\)](#)
  - A. Gould [ApJ 321, 571 \(1987\)](#)
  - ▶ Seismography: baryonic inertial mass
  - ▶ Neutrino absorption: weak charge, heavy mediator
  - ▶ Oscillations: non-universal flavor content, any mediator
- ▶ DM accumulation in the Earth could affect each case differently

# Key Points

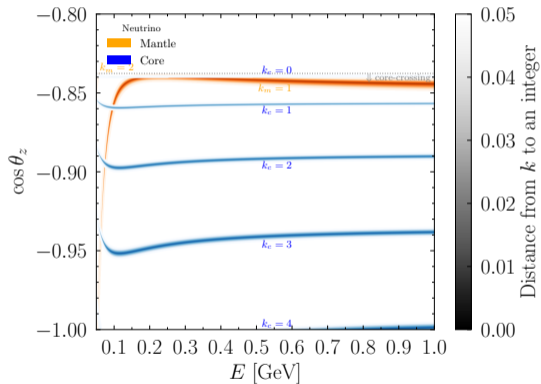
- ▶ Lots of tau neutrinos in atmospheric data sets
- ▶ Possible to identify them with a minimal number of assumptions
- ▶ Will be able to probe the Earth's core with oscillations with DUNE

Thanks!

# Backups

# Parametric Resonances

## Neutrinos:



## Antineutrinos:

